Last name:	First	name:	SID#:
Collaborators:			

CMPUT 609 Written 1: Step Sizes & Bandits

Due: Tuesday Sept 13 in Gradescope by 2pm (no slip days)

Policy: Can be discussed in groups (acknowledge collaborators) but must be written up individually. Submit a PDF file to Gradescope.

There are a total of 90 points on this assignment.

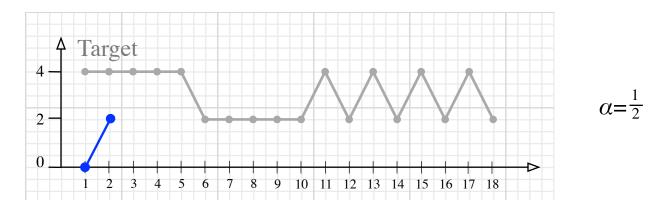
Question 1 [72 points] Step-sizes. Plotting recency-weighted averages.

Equation 2.5 (from the SB textbook, online 2nd edition) is a key update rule we will use throughout the course. This exercise will give you a better hands-on feel for how it works. This exercise has eight parts. There are 6 points for plotting each of the first four graphs, 3 points for plotting each of the second four graphs, and 3 points for answering each specific subquestion (everything ending with a question mark).

Do all the plots in this question by hand. You should not even need a calculator, as the numbers are easy to place by eye (using fractions instead of floating points might help). You will get a better feel for it if you place the points manually. To make it easy for you, I'll include some graphing area and a start on the first plot here, so you should just be able to print these pages out and draw on them. This question has 7 parts.

Part 1. (15 pts.)

Suppose the target is 4.0 for five steps, then 2.0 for five steps, and then alternates between 2.0 and 4.0 for 8 more steps, as shown by the grey line in the graph below. Suppose the initial estimate is 0.0, and that the step-size (in the equation) is 0.5. Your job is to apply Equation 2.5 iteratively to determine the estimates for time steps 2-19. Plot them on the graph below, using a blue pen, connecting the estimate points by a blue line. The first two estimate points are already marked and connected in dark blue (or black) below:

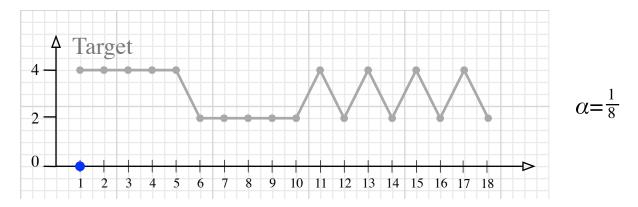


What is the estimate after 5 updating steps (i.e., on step 6)? Please give the number as a symbolic expression.

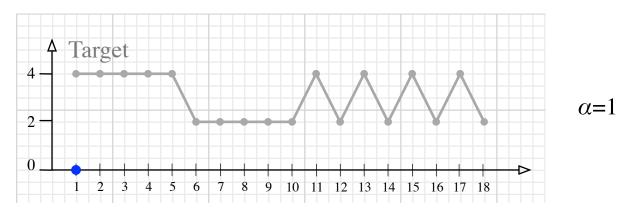
What would it be after 10 steps, if the target continued to be 4.0? Please give the number as a symbolic expression.

After 20 steps of a target of 4.0? Please give the number as a symbolic expression.

Part 2. (6 pts) Repeat the graphing/plotting portion of Part 1, this time with a step size of 1/8.



Part 3. (6 pts.) Repeat with a step size of 1.0.



Part 4. (6 pts.) Best step-size questions.

Which of these step sizes would produce estimates of smaller absolute error if the target continued alternating for a long time?

Which of these step sizes would produce estimates of smaller absolute error if the target remained constant for a long time?

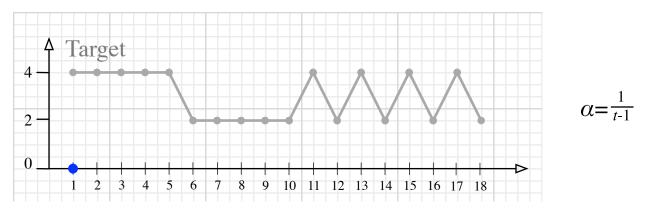
Part 5. (6 pts.)

Now suppose the target R_t moved randomly, such that $R_{t+1} = R_t + N(0,1)$ where N(0,1) is a normally distributed random variable with mean 0 and variance 1. In this case, which of these step sizes would produce estimates of smaller absolute error?

Part 6. (6 pts.)

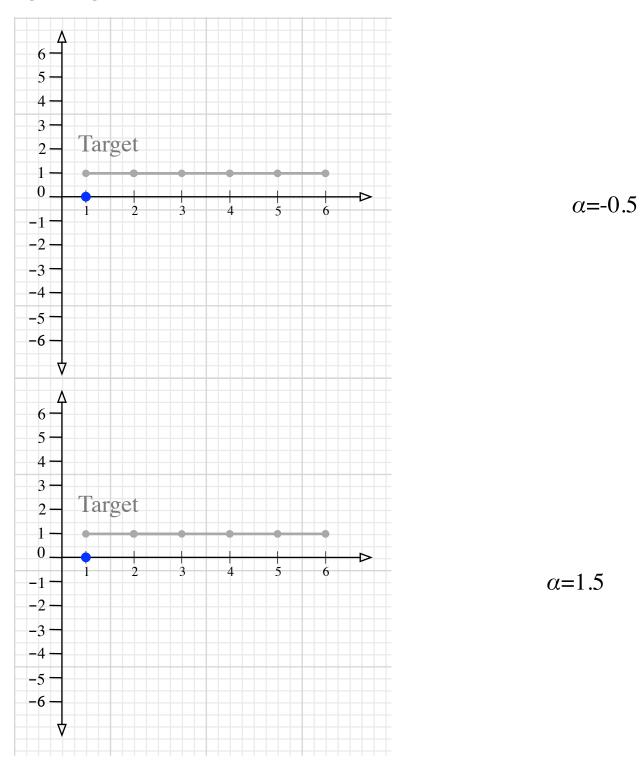
Now suppose the target was of the form $R_t = N(\mu_t, 1)$ a normally distributed random variable with mean μ_t and variance 1, and the mean moved randomly according to $\mu_{t+1} = \mu_t + N(0,1)$. Then which of these step sizes would produce estimates of smaller absolute error? If you are not completely sure which is best, then say what you are sure of about the best step size and explain your reasoning.

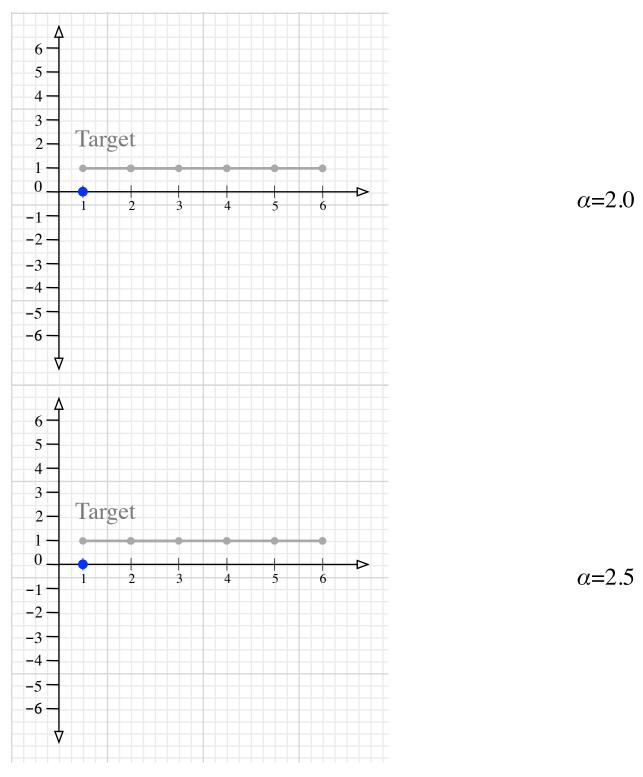
Part 7. (12 pts.) Repeat with a step size of 1/(t-1) (i.e., the first step size you will use is 1, the second is 1/2, the third is 1/3, etc.).



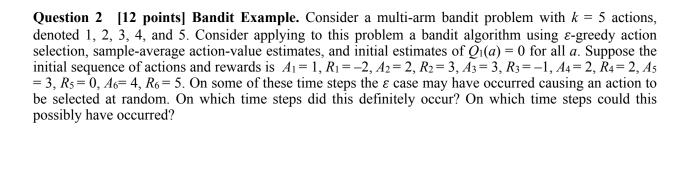
Based on all of these graphs, why is the 1/(t-1) step size appealing?

Part 8. (15 pts.) You might think that the step size should be between 0 and 1. Make plots for the first 6 steps with step sizes of -0.5, 1.5, 2.0, and 2.5.





What is the safe range for the step size? Explain.



The remaining question is an exercise from the Sutton and Barto textbook. Be sure to explicitly answer each subquestion posed in each exercise. These are the exercise numbers as given in the online text. Attach additional pages, as needed, for your answer.

2.4 [6 points] (Spikes in the optimistic-initialization graph)